RF SYSTEMS Written Test of June 17th, 2022



Exercise 1



The figure shows a terrestrial link operating at 24 GHz with bandwidth B=200 MHz. The two stations are located L km away and the antennas are both placed on top of 15 m high towers. The gain of both antennas is G=30 dB, the transmitted power from T is P_T =20 dBm and the equivalent noise temperature of the receiving station is T_{sys} =200 °K.

- 1) Evaluate the maximum value of L (L_{max}) due to the earth surface curvature
- 2) Assuming the antennas optimally pointed, evaluate the received power for $L=L_{max}$.
- 3) The required value of the signal-to-noise ratio (SNR_{sys}) at R must be ≥ 22 dB. Chose the largest value of L satisfying this requirement and compute the received power and the corresponding value of SNR_{sys}.

Consider the following scheme for the receiving station R:



- 4) Evaluate the equivalent noise temperature of the digital receiver (T_R) compatible with the imposed T_{sys}.
- 5) Assuming $E_b/N_0=20$ dB at the receiver output, what is the maximum data rate DR?

We want design a single stage amplifier at 10 GHz using the scheme in the following figure (input and output networks are lossless):



The transistor to be used has the following parameters: $S_{11}=0.57 \angle 166^{\circ}$ $S_{21}=2.59 \angle -21^{\circ}$ $S_{12}=0.144 \angle -50^{\circ}$ $S_{22}=0.39 \angle -148^{\circ}$ $\Gamma_{opt}=0.435 \angle 168^{\circ}$ $F_{min}=1.15$ dB $R_n=0.095$ (Noise parameters) 3^{th} order Intercept point (IP3): 26 dBm

The amplifier must exhibit the transducer gain as high as possible compatibly with the stability requirement and the noise figure not larger than 2 dB.

- 1) Select a proper value for Γ_s and Γ_L in order to satisfy the above requirements
- 2) Select as desired the topology of the input network and evaluate the values of the components
- 3) Assuming at input a 2-tone signal ($f_0=10$ GHz, $\Delta f=200$ MHz) with available mean power (Pin) equal to 0 dBm, evaluate the output mean power Pout. Compute also the power at each intermodulation frequency (specify the value of these frequencies)

We want to design the oscillator in the figure operating at 10 GHz. Assume the transmission lines (TEM) filled with a dielectric material having $\varepsilon_r=2.2$.



The S parameters of the active device at 10 GHz are given in the following table as function of the bias current:

Ibias	S11	S12	S21	S22
5 mA	0.745 ∠ -162.9°	0.063∠-7.1°	1.875∠25.1°	0.602∠-119.6°
10 mA	0.76∠-145°	0.06∠-1.2°	1.92∠43.6°	0.603∠-105.3°
15 mA	0.864∠-93.4°	0.064∠27.4°	2.545∠93.8°	0.627∠-64.2°

- 1) Select the bias current (checking the necessary condition for the oscillation)
- 2) Imposing $|\Gamma_{out}|=1.1$, evaluate the required Γ_s and the length L_{in} of the input line so that the oscillation can start.
- 3) Compute the reflection coefficient Γ_L to be presented at the transistor output and design the output network (i.e. evaluate the susceptances B_1 and B_2)

Solution

Exercise 1

The maximum value of L in Km is given by $L_{\text{max}} = 3.57 \cdot \left(\sqrt{H_1} + \sqrt{H_2}\right)$ with H₁=H₂=15m. It is found L_{max}=27.65 Km.

The received power at R is obtained from the Friis equation (in logarithmic units):

$$P_R = P_T - 20 \cdot \log\left(\frac{4\pi L}{\lambda}\right) + 2G$$
 with $\lambda = c/f_0 = 12.5$ mm. Replacing we get: $P_R = -68.78$ dBm.

The signal-to-noise ratio is defined as $SNR_{sys}=P_R/P_N$, with $P_N=KT_{sys}B=5.52\cdot10^{-13}$ (-92.58 dBm) the noise power at R. Imposing $SNR_{sys}=22$ dB we get $P_R=P_N SNR_{sys}=-70.58$ dBm. Replacing in the Friis equation the value of L can be derived: L=33.615 Km. This value is however largen than L_{max} , so the maximum value of L that can be chosen is $L=L_{max}=27.65$ Km. For this value we get $P_R=-68.78$ dBm and $SNR_{sys}=-68.78+92.58=23.8$ dB.

The expression of T_{sys} as function of the receiving front-end parameters is given by:

$$T_{sys} = T_a + T_f + a_f T_{LNA} + \frac{a_f T_R}{g_{LNA}} \text{ with } a_f = 10^{A_f/10}, \quad T_f = 293 \cdot (a_f - 1), \quad T_{LNA} = 293 \cdot (10^{NF_{LNA}/10} - 1), \quad g_{LNA} = 10^{G_{LNA}/10} .$$

Deriving T_R we get: $T_R = \frac{g_{LNA}}{a_f} \left(T_{sys} - \left(T_a + T_f + a_f T_{LNA} \right) \right) = 257.22 \text{ °K}.$

We know that SNR_{sys}=(E_b/N₀)(DR/B). Then, it has DR=B·SNR_{sys}/(E_b/N₀)=479.77 Mbit/sec.

After entering the transistor parameters in the S.C. we found that the device in potentially instable with Gmax=12.549 dB.

As the problem requires as minimum noise figure NF=2 dB, we draw on the S.C. the corresponding noise figure circle. Then we look for a point (Γ_S) on this circle determining the largest Available Gain (G_{AV}). This point is the one where the circle with constant G_{AV} is tangent to the circle with constant NF. It is found $\Gamma_S=0.648\angle$ -157.34° and G_{AV}=11.825 dB.

The value of Γ_L is obtained by imposing the conjugate matching at the transistor output. Using the S.C. we get $\Gamma_L=0.609 \ge 174.95^\circ$. Once this is imposed, it has $G_T=G_{AV}=11.825$ dB.

A single stub network can be easily designed for the input network:

The value of Γ_s is entered in the S.C. and stored in memory. The circle with constant gamma passing through the current point is drawn together with the circle with g=1. The first intersection of the two circles in the direction of the load is selected and the phase in the Delta Gamma tab gives the length of the transmission line: $\Phi=27.07/2=13.535^\circ$. The imaginary part of Y (current point) gives the value of b=1.695.

The value of Pout is given by Pout=Pin+ G_T =11.825 dBm. The power in each line is P_0 =11.825-3 = =8.825 dB. The power in the intermodulation lines is computed by the following formula: Pint=3P₀ -2IP3=-25.525 dBm.

The bias selection is carried out by checking the oscillation condition (potential instability). It is found that only for IB=15mA this condition is verified.

To select Γ_s , we draw the source mapping circle with $|\Gamma_{out}|=1.1$. Being Γ_s generated by a lossless network (the short-circuited stub), the point to be selected on this circle must be on the intersection with the outer circle ($|\Gamma_s|=1$). We have selected $\Gamma_s=1\angle 89.78^\circ$. Being generated by a S.C. stub, it holds true $\Gamma_s=\exp(\pi-2\phi_{in})$, where ϕ_{in} is the electrical length of the line: $\phi_{in}=\beta L_{in}=(\pi-\phi_s)/2$. From this latter we get: $L_{in} = \frac{\phi_{in}}{\beta} = \frac{c}{f_0\sqrt{\varepsilon_r}} \frac{\pi-\phi_s}{4\pi} = 2.534$ mm.

Once Γ_s is assigned, the value of Γ_{out} can be obtained by the S.C.: $\Gamma_{out} = 1.1 \angle -137.25^{\circ}$. yout is also available: $y_{out}=-0.346+j2.514$. We then assign $y_L=-g_{out}/3-b_{out}=0.115-j2.514$, which corresponds to $\Gamma_L=0.969 \angle 136.688^{\circ}$.

The design of the output network starts drawing the circle g=1 rotated by $2\beta L_{out}=270^{\circ}$ in the source direction, together with the circle with g=const passing trough Γ_L . The value of Γ_L is then entered and stored in memory. We select the first intersection between the two circles and read the value in the Delta Y tab (imaginary part). This value, with the sign reversed, represents b₁=-3.98. We then move the current point in the load direction by 270° and get as new current point y=1-j5.049. The value of b₂ is the imaginary part of y: b₂=-5.049.