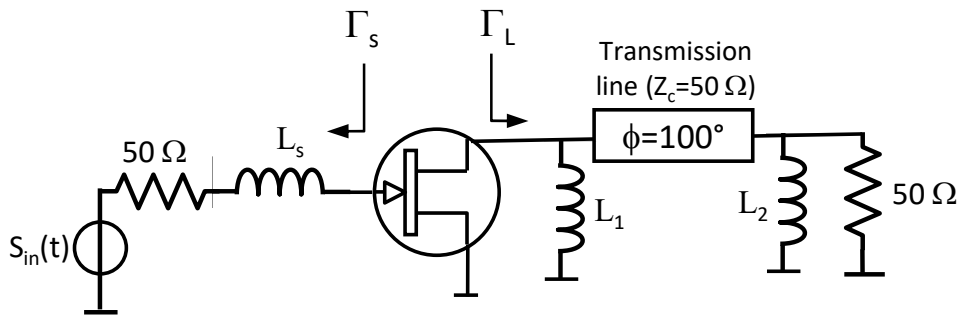


**RF SYSTEMS**  
**End Test on 21 January 2022**

<b>Surname &amp; Name</b>
<b>Identification Number</b>
<b>Signature</b>

Exercise 1

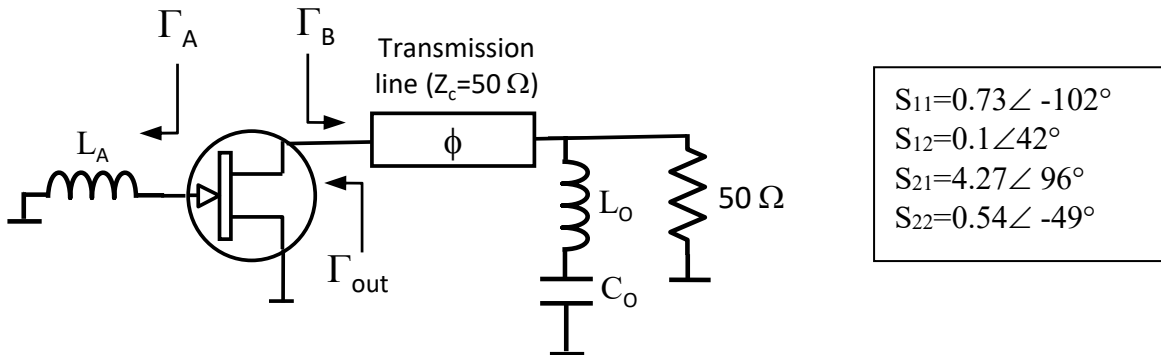
A power amplifier operating at 1.2 GHz with the scheme in the figure must be designed. The active device is characterized by the following S parameters:  $S_{11}=0.37\angle-160.8^\circ$ ,  $S_{21}=3.3\angle 23.68^\circ$ ,  $S_{12}=0.091\angle 22.9^\circ$ ,  $S_{22}=0.25\angle-91.7^\circ$ . The IP3 parameter of the device is also assigned:  $IP3=22$  dBm.



- 1) Assume  $S_{in}(t)$  a 2-tone signal with average power  $P_{in}=0$  dBm. Evaluate the average output power that determines the carrier-to-intermodulation (CI) of the output signal not smaller than 30 dB. Compute then the required transducer gain  $G_T$  (Note that this gain cannot exceed the maximum gain of the transistor).
- 2) The conjugate matching at the transistor output is assumed. Evaluate  $\Gamma_s$  and  $\Gamma_L$  so that the previously computed  $G_T$  is obtained. Note that  $\Gamma_s$  must be selected so that it can be realized with the assigned input network (Hint: the impedance  $Z_s$  corresponding to  $\Gamma_s$  is the series of  $50 \Omega$  with a positive reactance. Then, on the Smith Chart,  $\Gamma_s$  must be on a specific circle).
- 3) Compute the value of  $L_s$ ,  $L_1$  and  $L_2$  of the input and output networks. Note that only positive values are meaningful.

## Exercise 2

An oscillator working at  $f_0=1$  GHz must be designed with the scheme in the figure (the S parameters of the active device are also reported).



- 1) Imposing  $|\Gamma_{out}|=1.2$  evaluate  $\Gamma_A$  and  $\Gamma_B$  that allow the start of the oscillation (choose  $\Gamma_A$  so that it can be implemented with the largest value of the inductor  $L_A$ ). After  $\Gamma_A$  and  $\Gamma_B$  are obtained, check that the oscillation can actually start.
- 2) Compute the value of the inductor  $L_A$
- 3) The output network transforms the load ( $50 \Omega$ ) into  $\Gamma_B$ . Assuming that the series resonator resonates at  $f_r=2f_0$ , compute the electrical length  $\phi$  and the values of  $L_o$  and  $C_o$  of the output network. Hint: The resonator at  $f_0$  is represented by a susceptance whose value  $B$  is obtained by the design of the transforming network. To find  $L_o$  and  $C_o$  use the following expression:

$$B = \frac{1}{2\pi f_r L_o \left( \frac{f_r - f_0}{f_0} \frac{f_0}{f_r} \right)} > 0, \text{ with } f_r = \frac{1}{2\pi \sqrt{L_o C_o}} = 2f_0. \text{ Being } B > 0, \text{ this constraint must be}$$

taken into account during the design of the output network.

- 4) What is the advantage of using the series resonators in the output network?

## Solutions

### Exercise 1

From the S parameter we know that the device is unconditionally stable with  $G_{TMAX}=11.6$  dB.

1) The following equation should be used:  $CI_{dB} \approx 2IP_3 - 2P_m + 6$ , from which we get  $P_m=10$  dBm.

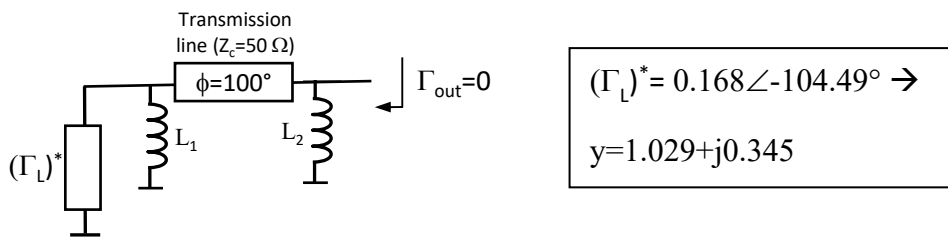
Being the input power 0 dBm, the required transducer gain is  $G_T=10$  dB (admissible because  $< G_{TMAX}$ ).

2) Being the matching at output imposed, we design the amplifier using the Available Power Gain. First, we draw the circle with  $G_{AV}=10$  dB and select a point on this circle (this point represents  $\Gamma_S$ ). The selection is not free because the input network imposes that the impedance  $z_S$  (corresponding to  $\Gamma_S$ ) must be in the form  $(1+jx_S)$ , with  $x_S>0$ . Then the selected point must be on the intersection of the  $G_{AV}$  circle with upper part of the circle  $r=1$ :  $\Gamma_S=0.314\angle 71.68^\circ$  (corresponding to  $z_S=1+j0.662$ ).

To have the  $G_{AV}$  equal to  $G_T$  we must then impose the conjugate matching at output. With the S.C. we get  $\Gamma_L=0.168\angle 104.49^\circ$ .

3) The inductance  $L_S$  is determined from  $X_S=50 \cdot x_S=50 \cdot 0.662=33.1 \Omega$ :  $L_S = X_S / (2\pi f) = 4.39$  nH.

To design the double stub network at output is convenient to consider the dual problem (matching  $\Gamma_{out} = (\Gamma_L)^*$  to 50 Ohm):

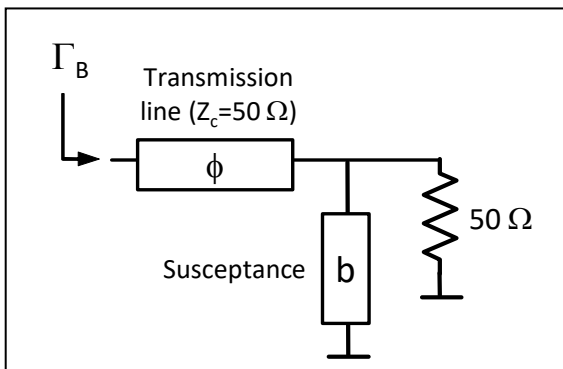


We start by inserting  $(\Gamma_L)^*$  in the S.C., store this value in memory and draw the circle  $g=1$  rotated by  $200^\circ$  in the load direction. Then select one of the two intersections of this circle with the circle  $g=\text{const}$  passing for the load ( $g=1.029$ ). The imaginary part of Delta Y represents the susceptance  $b_1=-0.477$ . Note that this value is acceptable being the susceptance implemented by an inductor. The value of  $L_1$  is obtained from:  $L_1 = -50 / (2\pi f b_1) = 13.9$  nH. Now we give an increment of  $-200^\circ$  to the current point to arrive at the input of the transmission line. This point must be on the circle  $g=1$ . In fact, from the S.C. we obtain  $y_2=1+j0.133$ . To arrive to the center of the S.C. the susceptance  $b_2=-0.133$  must then be added, which is realized by the inductance  $L_2 = -50 / (2\pi f b_2) = 49.86$  nH.

## Exercise 2

From the S parameter we get  $K=0.473 < 1$  then the device is potentially instable and suitable for the oscillator design.

- 1) We draw the  $\Gamma$ s mapping circle with  $|\Gamma_{out}|=1.2$ , which intersects the outer circle of the Smith Chart in two points. We select the one with the largest normalized reactance:  $\Gamma_A = 1 \angle 89.4^\circ$ . The output reflection coefficient results  $1.2 \angle -137.03^\circ$ , to which correspond the impedance  $z_{out} = -0.105 - 0.39i$ . To ensure the start of oscillation we assign  $z_B = 0.035 + 0.39i$ , corresponding to  $\Gamma_B = 0.941 \angle 137.35^\circ$ . To check the oscillation condition at the input of the transistor we determine the input reflection coefficient with the S.C. determined by  $\Gamma_B$ :  $|\Gamma_{in}| = 1.02$ . Being  $> 1$  both  $|\Gamma_{in}|$  and  $|\Gamma_{out}|$  the start of the oscillation is confirmed.
- 2) From  $\Gamma_A$  we derive with the S.C.  $x_A = 1.011$  and then  $X_A = 50 \cdot x_A = 50.55 \Omega$ . The inductance  $L_A$  is then given by:  $L_A = \frac{X_A}{2\pi f_0} = 8.0453 \text{ nH}$
- 3) The transforming network has the single stub topology. Assume the series resonator represented by its normalized susceptance  $b$ . As explained in the text, this susceptance must be positive. Starting from  $\Gamma_B$  we move on the circle with constant gamma in the load direction until arrive at the intersection with the circle  $g=1$  where the imaginary part of  $Y$  is positive. The variation of the phase of gamma ( $\Delta\phi = 62.43^\circ$ ) defines the electrical length of the line:  $\phi = \Delta\phi/2 = 31.21^\circ$ . The admittance in the direction of the load observed at the intersection is  $1 + jb = 1 + j5.56$ , then  $b = 5.56$ .



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Imposing:

$$B = \frac{1}{2\pi f_r L_o \left( \frac{f_r}{f_0} - \frac{f_0}{f_r} \right)} = 0.02 \cdot 5.56 = 0.1112,$$

we get:  $L_o = \frac{1}{2\pi \cdot 2 \cdot 0.1668 \cdot 10^9} = 0.48 \text{ nH}$ . From the resonance condition at  $f_r = 2 \text{ GHz}$  we obtain

$$C_o = \frac{1}{(2\pi \cdot f_r)^2 L_o} = 13.19 \text{ pF}.$$

- 4) The presence of the series resonator introduces a short circuit at the second harmonic frequency. In this way this harmonic is removed from the load voltage, improving the spectral purity of the oscillator.