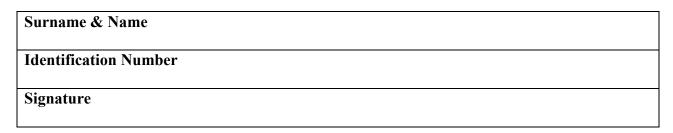
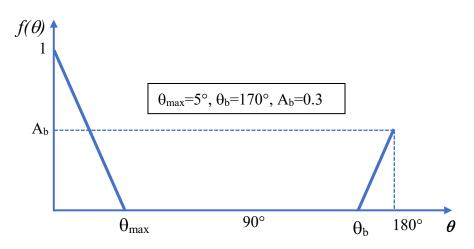
## RF SYSTEMS – 1<sup>th</sup> Midterm test 8 November 2018



Exercise 1



Consider the antenna exhibiting the directivity function  $f(\theta)$  shown in the figure (*f* is constant along the  $\varphi$  coordinate). Note that the part of *f* up to  $\theta_{max}$  represents the main lobe while that above 90° is the back lobe.

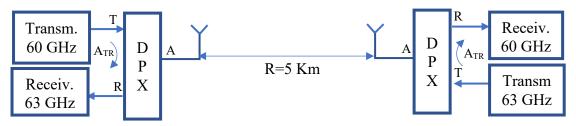
Analytically, *f* is expressed as follows:

 $f(\theta) = 1 - \theta/\theta_{\max} \text{ for } 0 < \theta < \theta_{\max}, \quad f(\theta) = A_b (\theta - \theta_b)/(\pi - \theta_b) \text{ for } \pi > \theta > \theta_b$  $f(\theta) = 0 \text{ elsewhere}$ 

- 1) Draw qualitatively the directivity diagram in the polar plane (f,  $\theta$  coordinate)
- 2) Compute the 3dB beam width  $\Delta \theta_{3dB}$  of the antenna (main lobe).
- 3) Compute the directivity gain  $D_M$  of the antenna. Hint:  $\int x \cdot \sin(x) \cdot dx = \sin(x) x \cdot \cos(x)$
- 4) The beam efficiency  $B_E$  is defined as the ratio of the power emitted in the main lobe and the emitted overall power. Evaluate  $B_E$  for the considered antenna.

Exercise 2

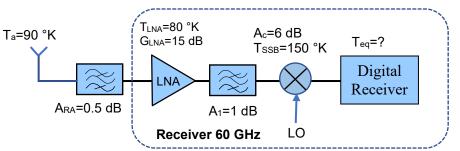
The full duplex communication system in the following figure operates at 60/63 GHz. The antennas are identical, with G=20 dB and  $T_a=90^{\circ}$ K



The block DPX is a diplexer, which allows connecting transmitters and receivers to a single antenna. The attenuation (dissipative) from ports T and R to port A is  $A_{TA}=A_{AR}=0.5$  dB. The rejection from port T to port R is  $A_{TR}=70$  dB. The signal is 256-QAM with B=32 MHz and the transmitted mean power (transmitters output) is  $P_T=40$  dBm. The transmitters produce intermodulation noise in the receiver band, determined by the ACPR=70 dB (which is the ratio between the power in the transmit band and the intermodulation power produced in the receiving band at the transmitters outputs).

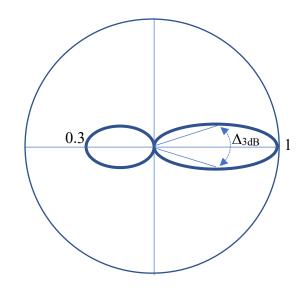
In addition to the free space attenuation  $L_f$  determined by R, an additional attenuation  $L_{add}=15$  dB must be included to account for meteorological events.

- 1) Evaluate the power at the input of the receiver at 60 GHz
- 2) Assuming that the receiving system temperature  $T_{sys}$  (antenna terminal) is 250 °K, evaluate SNR<sub>sys</sub>, which is defined as  $P_{ant}/(P_N+P_{int})$ , with  $P_{ant}$  the received power at antenna output,  $P_N$  the thermal noise power and  $P_{int}$  the intermodulation power in the receiving band arriving from the transmitter through A<sub>TR</sub> and reported at the antenna port.
- 3) With  $E_b/N_0=10$  dB, what is the allowed data rate *R*?
- 4) Consider the receiving path described in the following scheme:



Imposing  $T_{sys}$ =250 °K evaluate the maximum value for  $T_{eq}$  of the digital receiver. With the computed value of  $T_{eq}$ , is it possible, with a new value of T<sub>SSB</sub>, to remove the LNA and the following filter, maintaining the overall  $T_{sys}$  unchanged? Exercise 1

1)



2) Δθ<sub>3dB</sub> is obtained by imposing f(θ<sub>0.5</sub>)=0.5 → θ<sub>0.5</sub> = θ<sub>max</sub>/2=2.5°. Then Δθ<sub>3dB</sub> =2θ<sub>0.5</sub> =5°.
3) Computation of directivity gain D<sub>m</sub>:

$$D_{M} = \frac{4\pi}{\int_{0}^{2\pi} \int_{0}^{\pi} f(\theta) \sin(\theta) d\theta d\theta} = \frac{2}{\int_{0}^{\theta_{\max}} \int_{0}^{\pi} f_{1}(\theta) \sin(\theta) d\theta} = \frac{2}{\int_{0}^{\theta_{\max}} \int_{0}^{\pi} f_{1}(\theta) \sin(\theta) d\theta} = \frac{2}{\int_{0}^{\theta_{\max}} \int_{0}^{\pi} f_{1}(\theta) \sin(\theta) d\theta} = \frac{1}{\int_{0}^{\theta_{\max}} \int_{0}^{\pi} (1 - \frac{\theta}{\theta_{\max}}) \sin(\theta) d\theta} = 1 - \frac{\sin(\theta_{\max})}{\theta_{\max}} = 1.2687 \cdot 10^{-3}$$
$$\frac{1}{\theta_{0}} \int_{0}^{\pi} f_{2}(\theta) \sin(\theta) d\theta = \frac{A_{b}}{\pi - \theta_{b}} \int_{\theta_{b}}^{\pi} (\theta - \theta_{b}) \sin(\theta) d\theta = \frac{A_{b}}{\pi - \theta_{b}} (\pi - \theta_{b} - \sin(\theta_{b})) = 1.5208 \cdot 10^{-3}$$
$$D_{M} = \frac{2}{2.79 \cdot 10^{-3}} = 717 \quad (28.55 \text{ dB})$$

3)  $B_E$  is given by:

$$B_{E} = \frac{\int_{0}^{2\pi} \int_{0}^{\theta_{\text{max}}} f_{1}(\theta) \sin(\theta) d\phi d\theta}{\int_{0}^{2\pi} \int_{0}^{\pi} \int_{0}^{\pi} f(\theta) \sin(\theta) d\phi d\theta} = \frac{1.2687 \cdot 10^{-3}}{2.79 \cdot 10^{-3}} = 0.455$$

Exercise 2

1) Applying the Friis equation we get the received power at the receiver input (60 GHz):

$$P_r = P_t - A_{TA} + 2G - L_f - L_{add} - A_{AR} = 40 - 0.5 + 40 - 20 \log \left(\frac{4\pi \cdot 5000}{3 \cdot 10^8 / 60 \cdot 10^9}\right) - 15 - 0.5 = -77.98 \text{ dBm}$$

2) The received power at antenna terminal is  $P'_r=P_r+A_{AR}=-77.48 \text{ dBn} (1.7848 \cdot 10^{-11} \text{ W})$ . The thermal noise is  $P_N=KT_{sys}B=1.104 \cdot 10^{-13} \text{ W}$ . The intermodulation power at transmitter output is  $P_{int1}=P_t-ACPR=-30 \text{ dBm}$ . The intermodulation at the receiver input results:  $P_{int2}=P_{int1}-A_{TR}=-100 \text{ dBm}$ . This power, reported at the antenna terminal: Pint=Pint2+A\_{TA}=-99.5 \text{ dBm} (1.122 \cdot 10^{-13} \text{ W}) Finally:

$$SNR_{sys} = \frac{P_r'}{P_N + P_{int}} = \frac{1.7848 \cdot 10^{-11}}{1.104 \cdot 10^{-13} + 1.122 \cdot 10^{-13}} = 80.1797$$
 (19.04 dB)

3) It has:

$$SNR_{sys} = \frac{E_b}{N_0} \frac{R}{B} \implies R = B \frac{SNR_{sys}}{E_b/N_0} = 32 \cdot \frac{80.18}{10} = 256.58 \text{ Mbit/sec}$$

4) Expression of Tsys:

$$T_{sys} = T_a + T_{RA} + T_{LNA}A_{RA} + \frac{A_{RA}}{G_{LNA}} \left(T_1 + A_1T_{SSB} + T_{eq}A_1A_c\right) = 250$$

$$A_{RA} = 10^{0.05} = 1.122, A_1 = 10^{0.1} = 1.259, A_c = 10^{0.6} = 3.98$$

$$T_{RA} = T_0 \left(A_{RA} - 1\right) = 35.75 \ ^{\circ}K, \quad T_1 = T_0 \left(A_1 - 1\right) = 75.865 \ ^{\circ}K$$

$$0.1778 \cdot T_{eq} = 25.0951$$

$$T_{eq} = 141.12 \ ^{\circ}K$$
If the LNA and filter 2 are removed Tsys is expressed as:
$$T_{sys} = T_a + T_{RA} + A_{RA}T_{SSB} + T_{eq}A_{RA}A_c$$

Replacing the assigned parameters, even with  $T_{SSB}=0$ , we get  $T_{SSS}=756.1$  °K. Then it is not possible to eliminate the LNA maintaining  $T_{SSS}=250$  °K.