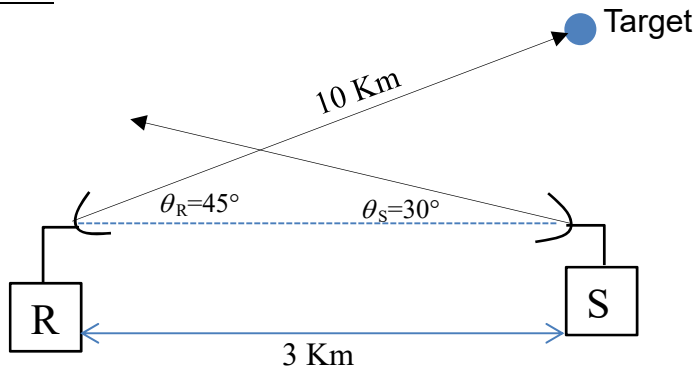


RF SYSTEMS
Written Test of February 25th, 2016

Surname & Name
Identification Number
Signature

Exercise 1



A discovery radar (R) operating at 4 GHz must be able to reveal a target at 10 Km and 45° elevation. The antenna used is a paraboloid dish with 1 m diameter (aperture efficiency $e_a=0.6$; efficiency $\eta=0.8$); the target is characterized by the radar cross section $\sigma=1\text{m}^2$. The transmitted power must be however limited by the presence, at the distance $L=3\text{ Km}$, of a satellite ground station (S) operating in the same frequency band. Also the antenna of S is a dish presenting a gain $G_S=40\text{ dB}$ with efficiency $\eta=0.9$, directed at 30° elevation (see the figure). Both antennas exhibit the same directivity function:

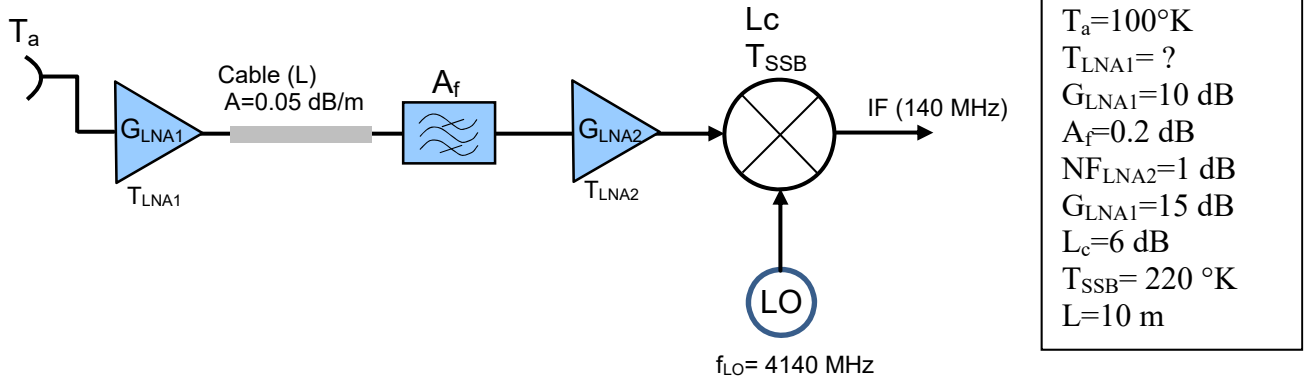
$$f(\theta) = \left[\frac{\sin(1.3915 \cdot \theta / \theta_{3dB})}{(1.3915 \cdot \theta / \theta_{3dB})} \right]^2 \quad (\theta \text{ is the angle with respect the maximum of } G).$$

θ_{3dB} is the angle where $f=0.5$ (remember that θ_{3dB} can be expressed, in a first approximation, as a function of D_{max})

- 1) Evaluate the gain G and the directivity gain D_{MAX} of the radar antenna
- 2) Evaluate θ_{3dB} for both antennas (R and S)
- 3) Compute the maximum transmitted power P_T from R in order that the received power by S don't exceed -50 dBm (note that R antenna is pointing in the direction of target)
- 4) Evaluate the sensitivity of the radar receiver (i.e. the received power generated by the considered target)

Exercise 2

Consider the RF front-end of the satellite receiving station of the previous exercise:

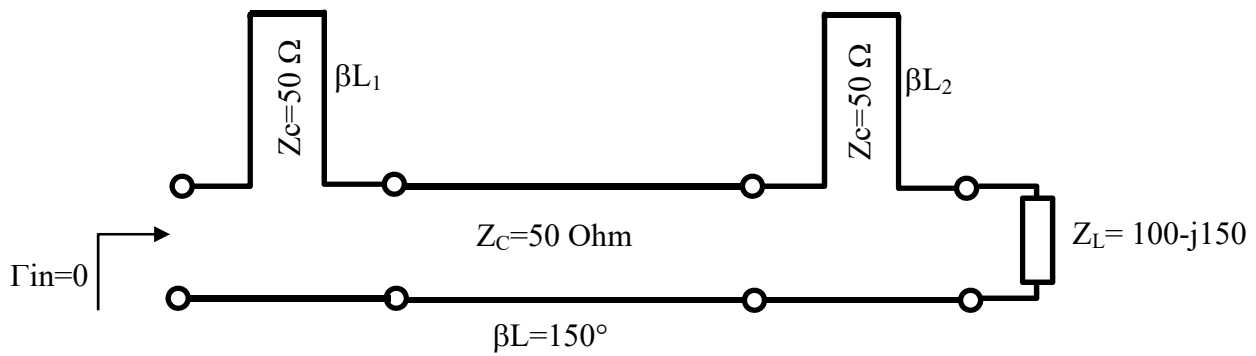


Assume for the received signal: $P_R = -60 \text{ dBm}$, $f_0 = 4.28 \text{ GHz}$, $B = 32 \text{ MHz}$.

- 1) Evaluate the signal power P_{IF} at IF output.
- 2) Write the expression of the equivalent noise temperature T_{eq} referred at the input of the RF front-end
- 3) Imposing $\text{SNR} = P_R / (K T_{\text{eq}} B) \geq 40 \text{ dB}$ evaluate the maximum value of T_{LNA1} .
- 4) Evaluate the noise power $P_{\text{N,IF}}$ at IF output: $P_{\text{N,IF}} = K T_{\text{IF}} B$, with T_{IF} the equivalent noise temperature at IF
- 5) Consider the disturbing signal at 4 GHz produced by the radar station at the antenna input ($P_{\text{RAD}} = -50 \text{ dBm}$). Evaluate the power $P_{\text{RAD,IF}}$ produced at IF output assuming the attenuation of the filter at the image frequency equal to 40 dB.
- 6) Assuming the disturbing signal at IF as noise, evaluate the overall signal-to-noise ratio at IF: $\text{SNR}_{\text{IF}} = P_{\text{IF}} / (P_{\text{N,IF}} + P_{\text{RAD,IF}})$

Exercise 3

Consider the matching network in the following figure.



Evaluate the electrical lengths βL_1 and βL_2 (choose the shortest lengths). Note that the stubs are connected in series and are terminated with a short circuit.

SOLUTION

Exercise 1

1) Gain of antenna R:

$$G = A_e \frac{4\pi}{\lambda^2} = e_a \left(\frac{\pi d}{\lambda} \right)^2$$

$$\lambda = 300 / 4 = 75 \text{ mm } (0.075 \text{ m}) \rightarrow G_R = 1050 \text{ (30.22 dB)}$$

$$D_{MAX} = G_R / \eta_R = 31.19 \text{ dB}$$

2) Evaluation of θ_{3dB} of the two antennas:

$$\theta_{3dB}^R = \frac{180}{\pi} \sqrt{\frac{4\pi}{D_{MAX}}} = 5.6^\circ$$

$$\theta_{3dB}^S = \frac{180}{\pi} \sqrt{\frac{\eta_s 4\pi}{G_S}} = 1.93^\circ$$

3) Link budget R→S:

$$P_{R,sat} = P_{T,rad} - 20 \log \left(\frac{4\pi \cdot 3 \text{ Km}}{\lambda} \right) + G_R + G_S + 10 \log (f_R (45^\circ)) + 10 \log (f_S (30^\circ)) = -50 \text{ dBm}$$

$$P_{T,rad} = 50.63 \text{ dBm}$$

4) Evaluation of the received power by R:

$$P_{R,rad} = P_{T,rad} - 2 \cdot 20 \log \left(\frac{4\pi \cdot 10 \text{ Km}}{\lambda} \right) + 2G_R + 10 \log \left(\frac{4\pi \cdot \sigma}{\lambda^2} \right) = -104.4 \text{ dBm}$$

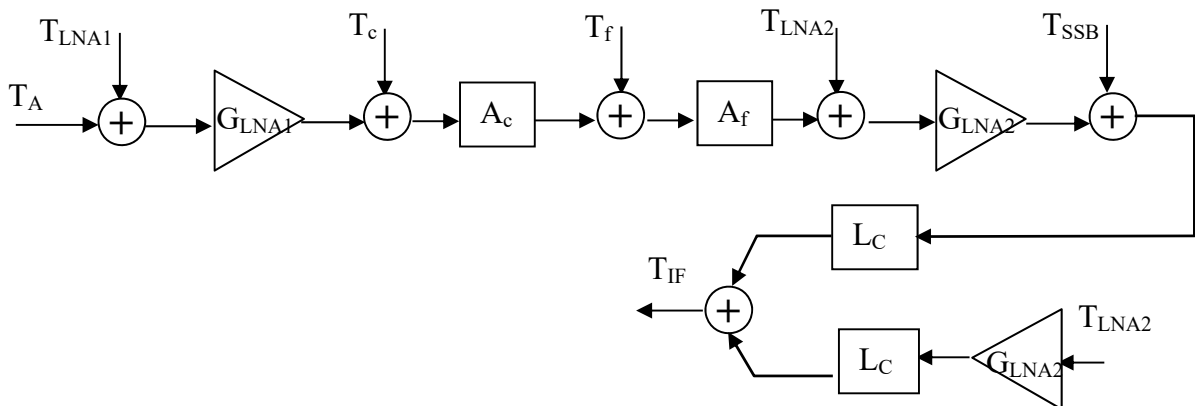
Exercise 2

1) Evaluation of Signal power at IF:

$$P_{R,IF} = P_R + G_{LNA1} - A \cdot 10 - A_f + G_{LNA2} - L_c = -41.7 \text{ dBm}$$

2) Expression of T_{eq} :

$$T_{eq} = T_a + T_{LNA1} + \frac{T_c}{G_{LNA1}} + \frac{T_f A_c}{G_{LNA1}} + 2 \frac{T_{LNA2} A_c A_f}{G_{LNA1}} + \frac{T_{SSB} A_c A_f}{G_{LNA1} G_{LNA2}}$$



$$T_{eq} = T_{LNA1} + 123.53$$

3) Evaluation of T_{LNA1} :

$$SNR = P_R - (KT_{eq}B)_{dB} = 40$$

$$(KT_{eq}B)_{dB} = -60 - 40 = -100 \text{ dBm} \rightarrow 10^{-13} \text{ W}$$

$$T_{eq} = \frac{10^{-13}}{KB} = 226.45 \text{ °K}$$

$$T_{LNA1} = T_{eq} - 123.53 = 102.92 \text{ °K}$$

4) Evaluation of $P_{N,IF}$:

$$T_{IF} = T_{eq} \frac{G_{LNA1} G_{LNA2}}{A_C A_f L_C} = 1.524 \cdot 10^4$$

$$P_{N,IF} = KT_{IF}B = 6.729 \cdot 10^{-12} \text{ W} \rightarrow -81.72 \text{ dBm}$$

5) Evaluation of $P_{RAD,IF}$:

$$P_{RAD,IF} = P_{RAD} + G_{LNA1} - A \cdot 10 - A_f(f_{IM}) + G_{LNA2} - L_c = -50 + 10 - 0.5 - 40 + 15 - 6 = -71.5 \text{ dBm}$$

6) Evaluation of SNR_{IF} :

$$P_{N,tot} = P_{N,IF} + P_{RAD,IF} = 10^{-81.72/10} + 10^{-71.5/10} = 7.752 \cdot 10^{-11} \rightarrow 71.1 \text{ dBm}$$

$$SNR_{IF} = P_{IF} - P_{N,tot} = -41.7 + 71.1 = 29.4 \text{ dBm}$$

Exercise 3

Using the electronic Smith Chart we get the reactances requested by the two stubs:

$$x_1 = -0.73$$

$$x_2 = 3.27$$

Using the expression $\phi = \tan^{-1}(x)$ we get the electrical lengths of the stubs:

$$\phi_1 = 143.72^\circ$$

$$\phi_2 = 73^\circ$$